

WE CLAIM:

1. A method for determining one or more signal parameters for a plurality of tones in an input signal, the method comprising:
 - 5 a) receiving samples of the input signal, wherein the input signal includes a plurality of tones;
 - b) generating a frequency transform of the samples, wherein the frequency transform comprises frequency response data for the plurality of tones;
 - c) determining one or more signal parameter estimates characterizing each of
10 the plurality of tones;
 - d) for each respective tone of the plurality of tones, generating modified frequency response data for the respective tone using one or more signal parameter estimates of one or more of the other tones, wherein the modified frequency response data for the respective tone includes reduced effects of other tones of the plurality of tones;
 - 15 wherein step d) is performed in an iterative fashion; and
 - e) determining final one or more signal parameter estimates for each of the plurality of tones based on the modified frequency response data of the plurality of tones.
2. The method of claim 1, wherein step c) comprises:
 - 20 c1) determining a plurality of potential local peaks based on the frequency response data, wherein each potential local peak corresponds to a tone;
 - c2) determining one or more signal parameter estimates characterizing each of the plurality of tones based on said plurality of potential local peaks;
 - c3) storing said one or more signal parameter estimates for each of the
25 plurality of tones;
3. The method of claim 2, wherein step d) comprises:

for each respective tone characterized by said one or more signal parameter estimates,

d1) removing effects of other tones of the plurality of tones from the frequency response data of the potential local peak of the respective tone using said one or more signal parameter estimates of each of said other tones to generate modified frequency response data for the respective tone;

d2) applying a single tone estimation method to the modified frequency response data, thereby generating a refined estimate of the one or more signal parameters of the respective tone; and

d3) updating said one or more signal parameter estimates with the refined estimate of the one or more signal parameters of the respective tone;

wherein, after said removing, said applying, and said updating for each tone, the one or more signal parameter estimates comprise refined estimates for each tone.

4. The method of claim 3, wherein step e) comprises:
performing steps d1) through d3) one or more times to generate final one or more signal parameter estimates for each of the plurality of tones.

5. The method of claim 4,
wherein said one or more signal parameter estimates characterizing the plurality of tones comprise a knowledge base of said signal parameter estimates;

wherein said storing one or more signal parameter estimates comprises:

storing a copy of said knowledge base, wherein said copy comprises a prior knowledge base; and

wherein said updating said one or more signal parameter estimates with the refined estimate of the one or more signal parameters of the respective tone comprises:

updating said knowledge base with said refined estimate of the one or more signal parameters of the tone, wherein, after said removing, said applying, and said

updating for each tone, the knowledge base is comprised of said refined estimates for each tone.

6. The method of claim 5, wherein said performing steps d1) through d3) one
5 or more times comprises performing steps d1) through d3) in an iterative manner until one or more of 1) the number of iterations exceeds a threshold number of iterations, and 2) the difference between values of the one or more signal parameters of said knowledge base and values of the one or more signal parameters of said prior knowledge base is less than a threshold value.

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7. The method of claim 4, wherein said one or more signal parameter estimates comprise estimates for one or more of frequency, amplitude, and phase.

8. The method of claim 7, wherein said estimate of frequency comprises the
15 frequency value of the determined potential local peak.

9. The method of claim 7, wherein said estimate of amplitude is zero.

10. The method of claim 7, wherein said estimate of amplitude is the value of
20 the potential local peak.

11. The method of claim 7, wherein said estimate of phase is zero.

12. The method of claim 4, wherein said frequency transform comprises a
25 windowed Fast Fourier Transform (FFT).

13. The method of claim 4, further comprising:
storing the final signal parameter estimates for each of the plurality of tones.

14. The method of claim 4, further comprising:
outputting the final signal parameter estimates for each of the plurality of tones.

5 15. The method of claim 4, wherein said storing said one or more signal
parameter estimates for each of the plurality of tones comprises:

sorting said signal parameter estimates for the plurality of tones by amplitude of
said potential local peaks; and

wherein said removing effects, said applying a single tone estimation, and said
10 updating said one or more signal parameter estimates are performed for each of said
plurality of tones in order of decreasing amplitude.

16. The method of claim 4, wherein said removing effects of other tones from
the frequency response data of the potential local peak of the respective tone comprises:

15 determining two or more sample values proximate to the potential local peak; and
for each of the other tones,

calculating an effect value for each of the two or more sample values using
the estimated signal parameters for the tone; and

subtracting the respective effect values from each of the two or more
20 sample values to generate a corresponding two or more modified sample values, wherein
said two or more modified sample values comprise said modified frequency response
data;

wherein said modified frequency response data are usable in applying said single
tone estimation method.

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17. The method of claim 16, wherein said two or more sample values are
consecutive sample values.

18. The method of claim 16,
wherein said frequency transform comprises a windowed Fast Fourier Transform (FFT) with window function $W(f)$, wherein f denotes frequency;

wherein said estimated signal parameters for the tone comprise an amplitude A_1 , a
5 frequency f_1 , and a phase ϕ_1 , and wherein said calculating an effect value for each of the
two or more sample values using the estimated signal parameters for the tone comprises
calculating:

$$dF(m) = A_1 e^{-j\phi_1} W(f_m + f_1) + A_1 e^{-j\phi_1} W(f_m - f_1),$$

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for each sample m , wherein m denotes an index of the sample, and f_m denotes the
frequency bin of the sample; and

wherein subtracting the respective effect value from each of the two or more
sample values comprises subtracting a respective value of $dF(m)$ from each of the two or
15 more sample values.

19. The method of claim 4, wherein said single tone estimation method
comprises:

identifying a frequency location proximate to an amplitude peak in the frequency
20 transform, wherein the amplitude peak corresponds to the tone;

selecting two or more frequency bins proximate to the frequency location in the
frequency transform; and

determining a tone frequency value that minimizes a difference between at least a
first expression and a second expression;

25 wherein the first expression comprises a sum of two or more numerator
terms divided by a sum of two or more denominator terms, wherein the first expression
includes a tone frequency variable;

wherein each numerator term and each denominator term corresponds to one of the frequency bins; and

wherein the second expression comprises a sum of one or more of the numerator terms divided by a sum of one or more of the denominator terms, wherein the
5 second expression includes the tone frequency variable;
wherein the tone frequency value comprises a frequency of the tone.

20. The method of claim 19,
wherein the tone frequency variable represents a correct tone frequency value of
10 the tone; and
wherein the determined tone frequency value represents an approximation of the correct tone frequency value.

21. The method of claim 20,
15 wherein the first expression is approximately equivalent to the second expression when the correct tone frequency value is used for the tone frequency variable in the first and second expressions.

22. The method of claim 19,
20 wherein a ratio of each numerator term and its corresponding denominator term represent an amplitude of the tone at a respective bin.

23. The method of claim 19,
wherein a ratio of each numerator term and its corresponding denominator term
25 represent a complex amplitude of the tone at a respective bin.

24. The method of claim 19,
wherein said determining a tone frequency value comprises:

computing a plurality of differences between the first expression and the second expression for different respective tone frequency values of the tone frequency variable; and

selecting the tone frequency value that produces a smallest difference.

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25. The method of claim 24, wherein said computing a plurality of differences comprises performing a Newton-Rhapson root finding method.

26. The method of claim 19,

10 wherein the first expression and the second expression are each a complex expression.

27. The method of claim 26,

15 wherein said determining a tone frequency value that minimizes a difference between a first complex expression and a second complex expression comprises determining a tone frequency value that minimizes a difference between an amplitude of the first complex expression and an amplitude of the second complex expression

28. The method of claim 19, wherein said frequency transform comprises a 20 windowed Fast Fourier Transform (FFT), and wherein the first expression and the second expression have the form:

$$\left| \frac{\sum_{k+1}^{k+M} (F(n)W^*(f_n - f_i) - F^*(n)W(f_n + f_i))}{\sum_{k+1}^{k+M} (|W(f_n - f_i)|^2 - |W(f_n + f_i)|^2)} \right| = \left| \frac{\sum_{k+1}^{k+M-1} (F(n)W^*(f_n - f_i) - F^*(n)W(f_n + f_i))}{\sum_{k+1}^{k+M-1} (|W(f_n - f_i)|^2 - |W(f_n + f_i)|^2)} \right|$$

25 wherein:

F(n) is the *n*th value of the single sided scaled FFT spectrum; and

W represents a window function, wherein the window function is shifted by a value of the tone frequency variable f_i .

29. The method of claim 19, wherein said frequency transform comprises a windowed Fast Fourier Transform (FFT), and wherein said generating a frequency transform of the samples comprises generating a power spectrum of the samples; wherein the first expression and the second expression have the form:

$$\left| \frac{\sum_{k+1}^{k+M} (|F(n)| \times |W(f_n - f_i)|)}{\sum_{k+1}^{k+M} |W(f_n - f_i)|^2} \right| = \left| \frac{\sum_{k+1}^{k+M-1} (|F(n)| \times |W(f_n - f_i)|)}{\sum_{k+1}^{k+M-1} |W(f_n - f_i)|^2} \right|$$

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wherein:

$F(n)$ is the n th value of the single sided scaled FFT spectrum; and

W represents a window function, wherein the window function is shifted by a value of the tone frequency variable f_i .

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30. The method of claim 19, further comprising:

computing one or more of the amplitude and phase of the tone using the determined tone frequency value.

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31. The method of claim 19,

wherein at least one of the two or more frequency bins is on each side of the frequency location.

32. The method of claim 19,

wherein said identifying comprises identifying a frequency location of at least one first magnitude peak in the frequency transform; and

wherein said selecting comprises selecting two or more frequency bins proximate to the at least one first magnitude peak in the frequency transform;

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33. The method of claim 4, wherein the frequency transform comprises a frequency transform array for the plurality of tones, and wherein said single tone estimation method comprises:

10 identifying a frequency location of at least one first magnitude peak in the frequency transform array;

selecting two or more frequency bins in a neighborhood of the at least one first magnitude peak in the frequency transform array; and

determining a tone frequency value that minimizes a difference between a first expression and a second expression;

15 wherein the first expression comprises a sum of two or more numerator terms divided by a sum of two or more denominator terms, wherein the first expression includes a tone frequency variable that represents a correct tone frequency value of the tone;

20 wherein each numerator term and each denominator term corresponds to one of the frequency bins; and

wherein the second expression comprises a sum of one or more of the numerator terms divided by a sum of one or more of the denominator terms, wherein the second expression includes a tone frequency variable that represents the correct tone frequency value of the tone;

25 wherein the determined tone frequency value represents an approximation of the correct tone frequency value.

34. The method of claim 33,

wherein the first expression is approximately equivalent to the second expression when the correct tone frequency value is used for the tone frequency variable in the first and second expressions.

5 35. The method of claim 33,
 wherein a ratio of each numerator term and its corresponding denominator term represent a complex amplitude of the tone at a respective bin.

 36. The method of claim 4, wherein said single tone estimation method
10 comprises:

 identifying two or more frequency bins proximate to a first magnitude peak in the frequency transform; and

 selecting a tone frequency value that makes a plurality of expressions most nearly equal;

15 wherein each of the plurality of expressions comprises a sum of one or more numerator terms divided by a sum of one or more denominator terms, wherein each of the plurality of expressions includes a tone frequency variable;

 wherein each numerator term and each denominator term corresponds to one of the frequency bins; and

20 wherein a ratio of each numerator term and its corresponding denominator term represent a complex amplitude of the tone at a respective bin; and

 wherein the tone frequency value comprises a frequency value of the tone.

 37. The method of claim 36,
25 wherein the tone frequency variable represents a correct tone frequency value of the tone; and

 wherein the determined tone frequency value represents an approximation of the correct tone frequency value.

38. The method of claim 37,
 wherein the first expression is approximately equivalent to the second expression
 when the correct tone frequency value is used for the tone frequency variable in the first
 5 and second complex expressions.

39. The method of claim 36,
 wherein said determining a tone frequency value comprises:
 computing a plurality of differences between the first expression and the
 10 second expression for different respective tone frequency values of the tone frequency
 variable; and
 selecting the tone frequency value that produces a smallest difference.

40. The method of claim 36,
 15 wherein a ratio of each numerator term and its corresponding denominator term
 represent a complex amplitude of the tone at a respective bin.

41. The method of claim 36, wherein said frequency transform comprises a
 windowed Fast Fourier Transform (FFT), and wherein the first expression and the second
 20 expression have the form:

$$\left| \frac{\sum_{k+1}^{k+M} (F(n)W^*(f_n - f_i) - F^*(n)W(f_n + f_i))}{\sum_{k+1}^{k+M} (|W(f_n - f_i)|^2 - |W(f_n + f_i)|^2)} \right| = \left| \frac{\sum_{k+1}^{k+M-1} (F(n)W^*(f_n - f_i) - F^*(n)W(f_n + f_i))}{\sum_{k+1}^{k+M-1} (|W(f_n - f_i)|^2 - |W(f_n + f_i)|^2)} \right|$$

wherein:
 25 F(n) is the *n*th value of the single sided scaled FFT spectrum; and

W represents a window function, wherein the window function is shifted by a value of the tone frequency variable f_i .

42. The method of claim 36, wherein said frequency transform comprises a windowed Fast Fourier Transform (FFT), and wherein said generating a frequency transform of the samples comprises generating a power spectrum of the samples; wherein the first expression and the second expression have the form:

$$\left| \frac{\sum_{k+1}^{k+M} (|F(n)| \times |W(f_n - f_i)|)}{\sum_{k+1}^{k+M} |W(f_n - f_i)|^2} \right| = \left| \frac{\sum_{k+1}^{k+M-1} (|F(n)| \times |W(f_n - f_i)|)}{\sum_{k+1}^{k+M-1} |W(f_n - f_i)|^2} \right|$$

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wherein:

$F(n)$ is the n th value of the single sided scaled FFT spectrum; and

W represents a window function, wherein the window function is shifted by a value of the tone frequency variable f_i .

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43. The method of claim 36, further comprising:
storing the determined tone frequency value in a memory.

44. The method of claim 36, further comprising:
outputting the determined tone frequency value.

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45. The method of claim 36, further comprising:
computing one or more of the amplitude and phase of the tone using the determined tone frequency value.

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46. The method of claim 36, wherein the plurality of expressions include:
a first expression comprising a sum of one or more numerator terms divided by a
sum of one or more denominator terms; and
a second expression comprising a sum of at least two numerator terms divided by
5 a sum of at least two denominator terms.

47. The method of claim 36, wherein the plurality of expressions include:
a first expression comprising a sum of two or more numerator terms divided by a
sum of two or more denominator terms; and
10 a second expression comprising a sum of three or more numerator terms divided
by a sum of three or more denominator terms.

48. The method of claim 1, further comprising:
determining a plurality of potential local peaks based on the frequency response
15 data for the plurality of tones, wherein each potential local peak corresponds to a tone;
wherein said one or more signal parameter estimates are determined based on the
plurality of potential local peaks;

49. The method of claim 1,
20 wherein said generating modified frequency response data for the respective tone
comprises generating modified frequency response data of the potential local peak of the
respective tone.

50. The method of claim 49, wherein said generating modified frequency
25 response data of the potential local peak comprises:
determining two or more sample values proximate to the potential local peak; and
for each of the other tones,

calculating an effect value for each of the two or more sample values using the estimated signal parameters for the tone; and

subtracting the respective effect values from each of the two or more sample values to generate a corresponding two or more modified sample values, wherein
5 said two or more modified sample values comprise said modified frequency response data.

51. The method of claim 50, wherein said two or more sample values are consecutive sample values.

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52. The method of claim 50,

wherein said frequency transform comprises a windowed Fast Fourier Transform (FFT) with window function $W(f)$, wherein f denotes frequency;

wherein said estimated signal parameters for the tone comprise an amplitude A_1 , a
15 frequency f_1 , and a phase ϕ_1 , and wherein said calculating an effect value for each of the two or more sample values using the estimated signal parameters for the tone comprises calculating:

$$dF(m) = A_1 e^{-j\phi_1} W(f_m + f_1) + A_1 e^{-j\phi_1} W(f_m - f_1),$$

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for each sample m , wherein m denotes an index of the sample, and f_m denotes the frequency bin of the sample; and

wherein subtracting the respective effect value from each of the two or more sample values comprises subtracting a respective value of $dF(m)$ from each of the two or
25 more sample values.

53. The method of claim 1, wherein, in each iteration of said generating modified frequency response data, (d) further comprises:

applying a single tone estimation method to the modified frequency response data, thereby generating a refined estimate of the one or more signal parameters of the

5 respective tone; and

updating said one or more signal parameter estimates with the refined estimate of the one or more signal parameters of the respective tone;

wherein the final one or more signal parameter estimates for each of the plurality of tones are determined based on the refined estimates of the one or more signal parameters of the respective tone.

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54. The method of claim 1, further comprising:

for each respective tone of the plurality of tones:

applying a single tone estimation method to the modified frequency response data, thereby generating a refined estimate of the one or more signal parameters of the respective tone; and

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updating said one or more signal parameter estimates with the refined estimate of the one or more signal parameters of the respective tone;

wherein said applying and said updating are performed for each of the plurality of tones in an iterative fashion; and

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wherein the final one or more signal parameter estimates for each of the plurality of tones are determined based on the refined estimates of the one or more signal parameters of the respective tone.

55. The method of claim 54, wherein said single tone estimation method comprises:

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identifying a frequency location proximate to an amplitude peak in the frequency transform, wherein the amplitude peak corresponds to the tone;

selecting two or more frequency bins proximate to the frequency location in the frequency transform; and

determining a tone frequency value that minimizes a difference between at least a first expression and a second expression;

5 wherein the first expression comprises a sum of two or more numerator terms divided by a sum of two or more denominator terms, wherein the first expression includes a tone frequency variable;

 wherein each numerator term and each denominator term corresponds to one of the frequency bins; and

10 wherein the second expression comprises a sum of one or more of the numerator terms divided by a sum of one or more of the denominator terms, wherein the second expression includes the tone frequency variable; and

 wherein the tone frequency value comprises a frequency of the tone.

15 56. The method of claim 55, wherein said determining a tone frequency value comprises:

 computing a plurality of differences between the first expression and the second expression for different respective tone frequency values of the tone frequency variable; and

20 selecting the tone frequency value that produces a smallest difference;

 wherein said computing a plurality of differences comprises performing a Newton-Rhapson root finding method.

25 57. A memory medium comprising program instructions for determining one or more signal parameters for a plurality of tones in an input signal, wherein the program instructions are executable by one or more processors to implement:

a) receiving samples of the input signal, wherein the input signal includes a plurality of tones;

b) computing a frequency transform of the input signal using said samples, wherein the frequency transform comprises frequency response data for the plurality of tones;

c) determining a plurality of potential local peaks based on the frequency response data, wherein each potential local peak corresponds to a tone;

d) determining one or more signal parameter estimates characterizing each of the plurality of tones based on said plurality of potential local peaks;

e) storing said one or more signal parameter estimates for each of the plurality of tones;

f) for each respective tone characterized by said one or more signal parameter estimates:

f1) removing effects of other tones of the plurality of tones from the frequency response data of the potential local peak of the respective tone using the stored one or more signal parameter estimates of each of said other tones, thereby generating modified frequency response data for the respective tone;

f2) applying a single tone estimation method to the modified frequency response data of the respective tone, thereby generating a refined estimate of the one or more signal parameters of the respective tone; and

f3) updating said one or more signal parameter estimates of the respective tone with said refined estimate;

wherein, after said removing, said applying, and said updating for each tone, the one or more signal parameter estimates comprise refined estimates for each tone;

g) performing step f) one or more times to generate final one or more signal parameter estimates for each of the plurality of tones.

58. The memory medium of claim 57,

wherein the one or more signal parameter estimates characterizing the plurality of tones comprise a knowledge base of said signal parameter estimates;

wherein said storing one or more signal parameter estimates comprises:

storing a copy of said knowledge base, wherein said copy comprises a
5 prior knowledge base; and

wherein said updating said one or more signal parameter estimates with the refined estimate of the one or more signal parameters of the respective tone comprises:

updating the knowledge base with said refined estimate of the one or more
signal parameters of the tone, wherein, after said removing, said applying, and said
10 updating for each tone, the knowledge base is comprised of said refined estimates for
each tone.

59. The memory medium of claim 58, wherein said performing step f) one or more times comprises performing step f) in an iterative manner until one or more of 1)
15 the number of iterations exceeds a threshold number of iterations, or 2) the difference
between values of the one or more signal parameters of said knowledge base and values
of the one or more signal parameters of said prior knowledge base is less than a threshold
value.

20 60. The memory medium of claim 57, wherein said one or more signal
parameter estimates comprise estimates for one or more of frequency, amplitude, and
phase.

61. The memory medium of claim 60, wherein said estimate of frequency
25 comprises the frequency value of the determined potential local peak.

62. The memory medium of claim 60, wherein said estimate of amplitude is
zero.

63. The memory medium of claim 60, wherein said estimate of amplitude is the value of the potential local peak.

5 64. The memory medium of claim 60, wherein said initial estimate of phase is zero.

65. The memory medium of claim 57, wherein said frequency transform comprises a windowed Fast Fourier Transform (FFT).

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66. The memory medium of claim 57, wherein said storing said one or more signal parameter estimates for each of the plurality of tones comprises:

 sorting said signal parameter estimates for the plurality of tones by amplitude of said potential local peaks;

15 wherein said removing effects, said applying a single tone estimation, and said updating said one or more signal parameter estimates are performed for each of said plurality of tones in order of decreasing amplitude of said potential local peaks.

67. The memory medium of claim 57, wherein said removing effects of other
20 tones from the frequency response data of the potential local peak of the respective tone comprises:

 determining two or more sample values in a neighborhood of the potential local peak; and

 for each of the other tones,

25 computing an effect value for each of the two or more sample values using the estimated signal parameters for the tone; and

 subtracting the respective effect value from each of the two or more sample values to generate a corresponding two or more modified sample values, wherein

said two or more modified sample values comprise said modified frequency response data; and

wherein said modified frequency response data are usable in applying said single tone estimation method.

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68. The memory medium of claim 67, wherein said two or more sample values are consecutive sample values.

69. The memory medium of claim 67,

10 wherein said frequency transform comprises a windowed Fast Fourier Transform (FFT) with window function $W(f)$, wherein f denotes frequency;

wherein said estimated signal parameters for the tone comprise an amplitude A_I , a frequency f_I , and a phase ϕ_I , and wherein said computing an effect value for each of the two or more sample values using the estimated signal parameters for the tone comprises

15 computing:

$$dF(m) = A_I e^{-j\phi_I} W(f_m + f_I) + A_I e^{-j\phi_I} W(f_m - f_I),$$

20 for each sample m , wherein m denotes an index of the sample, and f_m denotes the frequency bin of the sample; and

wherein subtracting the respective effect value from each of the two or more sample values comprises subtracting a respective value of $dF(m)$ from each of the two or more sample values.

25 70. The memory medium of claim 57, wherein said single tone estimation method comprises:

identifying a frequency location proximate to an amplitude peak in the frequency transform, wherein the amplitude peak corresponds to the tone;

selecting two or more frequency bins proximate to the frequency location in the frequency transform;

5 determining a tone frequency value that minimizes a difference between at least a first expression and a second expression,

 wherein the first expression comprises a sum of two or more numerator terms divided by a sum of two or more denominator terms, wherein the first expression includes a tone frequency variable;

10 wherein each numerator term and each denominator term corresponds to one of the frequency bins; and

 wherein the second expression comprises a sum of one or more of the numerator terms divided by a sum of one or more of the denominator terms, wherein the second expression includes a tone frequency variable which represents a correct tone

15 frequency value of the tone; and

 wherein the tone frequency value comprises a frequency of the tone.

71. The memory medium of claim 70,

 wherein the tone frequency variable represents a correct tone frequency value of
20 the tone; and

 wherein the determined tone frequency value represents an approximation of the correct tone frequency value.

72. The memory medium of claim 70,

25 wherein a ratio of each numerator term and its corresponding denominator term represent a complex amplitude of the tone at a respective bin.

73. The memory medium of claim 70, wherein the first expression and the second expression have the form:

$$\left| \frac{\sum_{k+1}^{k+M} (F(n)W^*(f_n - f_i) - F^*(n)W(f_n + f_i))}{\sum_{k+1}^{k+M} (|W(f_n - f_i)|^2 - |W(f_n + f_i)|^2)} \right| = \left| \frac{\sum_{k+1}^{k+M-1} (F(n)W^*(f_n - f_i) - F^*(n)W(f_n + f_i))}{\sum_{k+1}^{k+M-1} (|W(f_n - f_i)|^2 - |W(f_n + f_i)|^2)} \right|$$

wherein:

F(n) is the *n*th value of the single sided scaled FFT spectrum; and

W represents a window function, wherein the window function is shifted by a value of the tone frequency variable *f_i*.

74. The memory medium of claim 70,

wherein said generating a frequency transform of the samples comprises generating a power spectrum of the samples;

wherein the first expression and the second expression have the form:

$$\left| \frac{\sum_{k+1}^{k+M} (|F(n)| \times |W(f_n - f_i)|)}{\sum_{k+1}^{k+M} |W(f_n - f_i)|^2} \right| = \left| \frac{\sum_{k+1}^{k+M-1} (|F(n)| \times |W(f_n - f_i)|)}{\sum_{k+1}^{k+M-1} |W(f_n - f_i)|^2} \right|$$

wherein:

F(n) is the *n*th value of the single sided scaled FFT spectrum; and

W represents a window function, wherein the window function is shifted by a value of the tone frequency variable *f_i*.

75. The memory medium of claim 57, further comprising:

storing the final signal parameter estimates for each of the plurality of tones.

76. The memory medium of claim 57, further comprising:
outputting the final signal parameter estimates for each of the plurality of tones.

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77. The memory medium of claim 57, wherein the frequency transform comprises a frequency transform array for the plurality of tones, and wherein said single tone estimation method comprises:

identifying two or more frequency bins proximate to a first magnitude peak in the
10 frequency transform array;

determining a tone frequency value that minimizes a difference between a first expression and a second expression; and

selecting a tone frequency value that makes a plurality of expressions most nearly equal;

15 wherein each of the plurality of expressions comprises a sum of one or more numerator terms divided by a sum of one or more denominator terms, wherein each of the plurality of expressions includes a tone frequency variable;

wherein each numerator term and each denominator term corresponds to one of the frequency bins; and

20 wherein a ratio of each numerator term and its corresponding denominator term represent a complex amplitude of the tone.

78. A tone detection system, comprising:

25 an input for receiving samples of an input signal, wherein the input signal includes a plurality of tones;

a processor; and

a memory medium coupled to the processor, wherein the memory medium stores a tone detection software program for detecting the plurality of tones present in the input signal;

5 wherein the processor is operable to execute the tone detection software program to implement:

a) generating a frequency transform of the samples, wherein the frequency transform comprises frequency response data for the plurality of tones;

b) determining a plurality of potential local peaks based on the frequency response data, wherein each potential local peak corresponds to a tone;

10 c) determining one or more signal parameter estimates characterizing each of the plurality of tones based on said plurality of potential local peaks;

d) storing said one or more signal parameter estimates for each of the plurality of tones;

15 e) for each respective tone characterized by said one or more signal parameter estimates,

e1) removing effects of other tones of the plurality of tones from the frequency response data of the potential local peak of the respective tone using said one or more signal parameter estimates of each of said other tones to generate modified frequency response data for the respective tone;

20 e2) applying a single tone estimation method to the modified frequency response data, thereby generating a refined estimate of the one or more signal parameters of the respective tone; and

e3) updating said one or more signal parameter estimates with the refined estimate of the one or more signal parameters of the respective tone;

25 wherein, after said removing, said applying, and said updating for each tone, the one or more signal parameter estimates comprise refined estimates for each tone; and

f) performing step e) one or more times to generate final one or more signal parameter estimates for each of the plurality of tones.

79. The tone detection system of claim 78, wherein said removing effects of other tones from the frequency response data of the potential local peak of the respective tone comprises:

- 5 determining two or more sample values proximate to the potential local peak;
for each of the other tones,
calculating an effect value for each of the two or more sample values using
the estimated signal parameters for the tone; and
subtracting the respective effect value from each of the two or more
10 sample values to generate a corresponding two or more modified sample values, wherein
said two or more modified sample values comprise said modified frequency response
data; and
wherein said modified frequency response data are usable in applying said single
tone estimation method.

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80. The tone detection system of claim 79, wherein said two or more sample values are consecutive sample values.

81. The tone detection system of claim 79,
20 wherein said frequency transform comprises a windowed Fast Fourier Transform
(FFT) with window function $W(f)$, wherein f denotes frequency;
wherein said estimated signal parameters for the tone comprise an amplitude A_1 , a
frequency f_1 , and a phase ϕ_1 , and wherein said calculating an effect value for each of the
two or more sample values using the estimated signal parameters for the tone comprises
25 calculating:

$$dF(m) = A_1 e^{-j\phi_1} W(f_m + f_1) + A_1 e^{-j\phi_1} W(f_m - f_1),$$

for each sample m , wherein m denotes an index of the sample, and f_m denotes the frequency bin of the sample; and

wherein subtracting the respective effect value from each of the two or more sample values comprises subtracting a respective value of $dF(m)$ from each of the two or more sample values.

82. The tone detection system of claim 78, wherein said single tone estimation method comprises:

10 identifying an amplitude peak in the frequency transform, wherein the amplitude peak corresponds to the tone;

selecting two or more frequency bins in a neighborhood of the amplitude peak in the frequency transform; and

15 determining a tone frequency value that minimizes a difference between at least a first expression and a second expression;

wherein the first expression comprises a sum of two or more numerator terms divided by a sum of two or more denominator terms, wherein the first expression includes a tone frequency variable;

20 wherein each numerator term and its corresponding denominator term corresponds to one of the frequency bins; and

wherein the second expression comprises a sum of one or more of the numerator terms divided by a sum of one or more of the denominator terms, wherein the second expression includes the tone frequency variable; and

25 wherein the first expression is approximately equivalent to the second expression when the correct tone frequency value is used for the tone frequency variable in the first and second expressions; and

wherein the tone frequency value comprises a frequency of the tone.

83. The tone detection system of claim 82,
wherein the tone frequency variable represents a correct tone frequency value of
the tone; and

wherein the determined tone frequency value represents an approximation of the
5 correct tone frequency value.

84. The tone detection system of claim 82,
wherein a ratio of each numerator term and its corresponding denominator term
represent an amplitude of the tone at a respective bin.

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85. The tone detection system of claim 82,
wherein a ratio of each numerator term and its corresponding denominator term
represent a complex amplitude of the tone at a respective bin.

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86. A method for determining signal parameters for a plurality of tones in an
input signal, the method comprising:

a) receiving samples of the input signal, wherein the input signal includes a
plurality of tones;

20 b) applying a windowed FFT to the signal to generate a frequency transform
of the signal, wherein the frequency transform comprises frequency response information;

c) determining a plurality of potential local peaks based on the frequency
response information, wherein each potential local peak corresponds to a tone;

25 d) building a knowledge base of signal parameters characterizing said
plurality of tones by determining initial estimates of signal parameters for each of the
plurality of tones;

e) storing a copy of said knowledge base of tone parameters, wherein said
copy comprises a prior knowledge base;

- f) for each respective tone characterized in said knowledge base,
- f1) removing effects of the others of the plurality of tones from said estimates of the signal parameters using said knowledge base to generate modified frequency response information for the respective tone;
- 5 f2) applying a single tone estimation method to the modified frequency response information, thereby generating a refined estimate of the signal parameters of the tone; and
- f3) updating said knowledge base with said refined estimate of the signal parameters of the tone;
- 10 wherein, after said removing, said applying, and said updating for each tone, the knowledge base is comprised of said refined estimates for each tone; and
- g) performing steps e) through i) in an iterative manner until 1) the number of iterations exceeds a threshold number of iterations, or 2) the difference between values of the signal parameters of said knowledge base and values of the signal parameters of said
- 15 prior knowledge base is less than a threshold value.

87. A memory medium comprising program instructions for determining one or more signal parameters for a plurality of tones in an input signal, wherein the program

20 instructions are executable by one or more processors to implement:

- a) receiving the input signal, wherein the input signal includes a plurality of tones;
- b) computing a frequency transform of the input signal, wherein the frequency transform comprises frequency response data for the plurality of tones;
- 25 c) determining one or more signal parameter estimates characterizing each of the plurality of tones based on said frequency response data;
- d) for each respective tone of the plurality of tones, generating modified frequency response data for the respective tone using the one or more signal parameter

estimates of one or more of the other tones, wherein said generating the modified frequency response data for the respective tone removes effects of other tones of the plurality of tones;

wherein step d) is performed in an iterative fashion; and

- 5 e) determining final one or more signal parameter estimates for each of the plurality of tones based on the modified frequency response data of the plurality of tones.